



# ***Flat Optics based on Metasurfaces***

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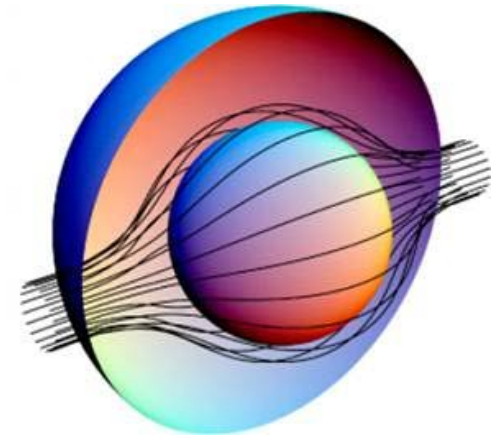
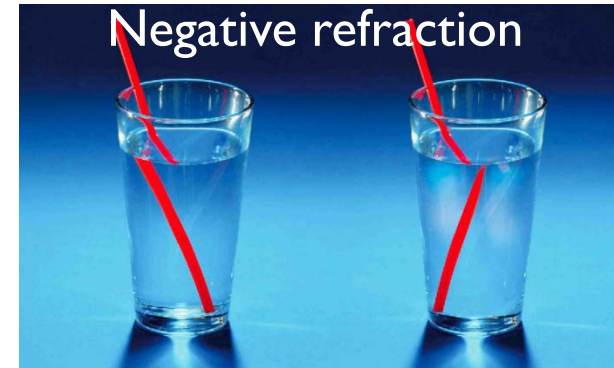
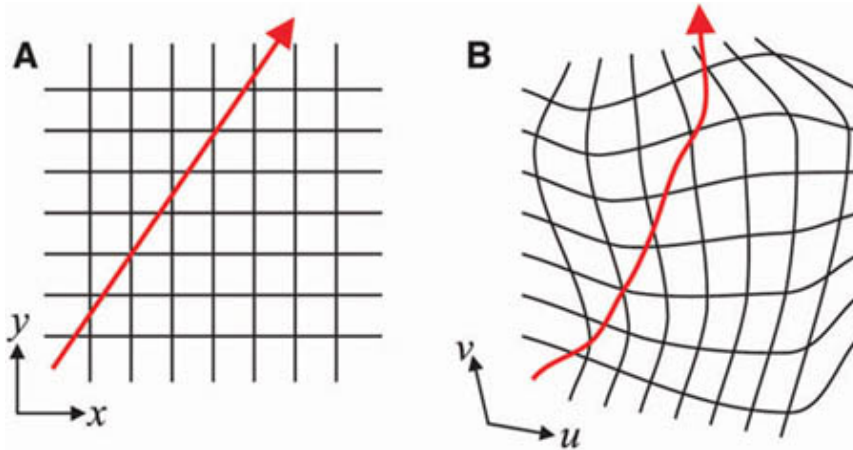
Review :

N.Yu and F. Capasso ,“Flat Optics with Designer  
Metasurfaces”

*Nature Materials* **13**, 139 (2014)

# METAMATERIALS

## Metamaterials and Transformation Optics



Optical cloaking

Viktor G Veselago 1968 *Sov. Phys. Usp.* **10** 509  
A.J. Ward and J.B. Pendry, *J. Mod. Opt.* **43** (1996)  
J.B. Pendry, D. Schurig and D.R. Smith, *Science* 312, 1780 (2006)

Propagation of light is controlled by considering artificial 3D materials with designed permittivity and permeability.

What can we do in 2D ? “metasurfaces”

# The Vision of Flat Optics

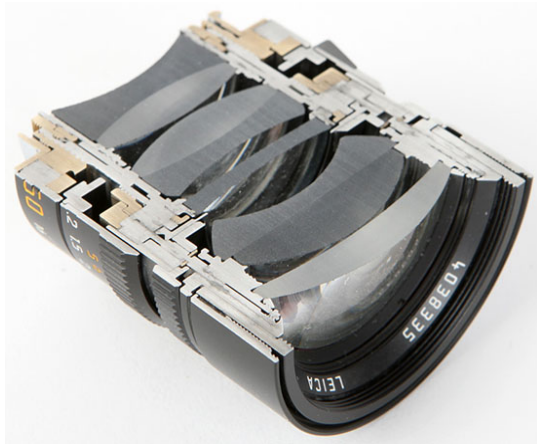
- Planar technology is central to Integrated Circuit technology ( \$ 300 B industry):  
Technology platform.
- Because of fabrication complexity 3D optical materials (metamaterials etc.) don't have a good chance of a major technology impact (large scale applications) at optical wavelengths.
- Ho do I know? From Photonic Crystals: exciting science but very limited technology penetration
- **So we should look at what we can do in 2D with metasurfaces**

## **METASURFACES FOR FLAT OPTICS**

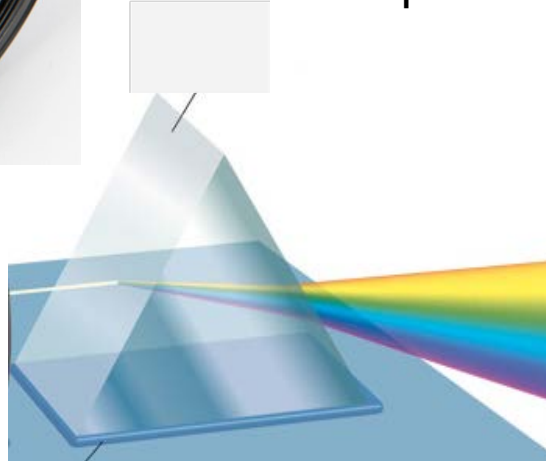
- Optically thin engineered metasurfaces for Wave Front Engineering (phase control):
- Local phase, amplitude and polarization control of light along the surface using optical resonators
- New class of flat, compact and broadband components:(lenses, polarizers, etc.), beyond conventional diffractive optics
- **Optical phased arrays for high speed wavefront control**

# Can we replace optical components with flat ones?

## Diffractive Optics



Conventional Optics



Optically thin subwavelength structured interface (metasurface)

**Metasurface:** an optically thin ( $\ll \lambda$ ) array of sub-wavelength size ( $\ll \lambda$ ), sub-wavelength ( $\ll \lambda$ ) spaced optical elements (resonators, antennas)

# Questions

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- ▶ Can we create metasurfaces that transform an incident beam into arbitrarily shaped (complex) beams (vortex, non-diffracting, etc. including vector beams) ?
- ▶ Can we make rapidly reconfigurable metasurfaces for fast wavefront control (nanosecond, many orders of magnitude faster than Spatial Light Modulators)?
- ▶ Can we make a high N.A. flat lens without aberrations (spherical, coma, etc.) and acromatic?
- ▶ Metasurface-based optical components : flat optics versus Fresnel Optics?
- ▶ Can we create metasurfaces that generate broadband vector beams (amplitude, phase and polarization vary from point to point)?
- ▶ Are strong optical interference effects possible in films much thinner than the wavelength (metafilms)?
- ▶ Physics and Technology of Disordered Metamaterials?
- ▶ What interesting physics and applications can emerge from embedding quantum effects into metasurfaces?
- ▶ Which large area lithographic technique?

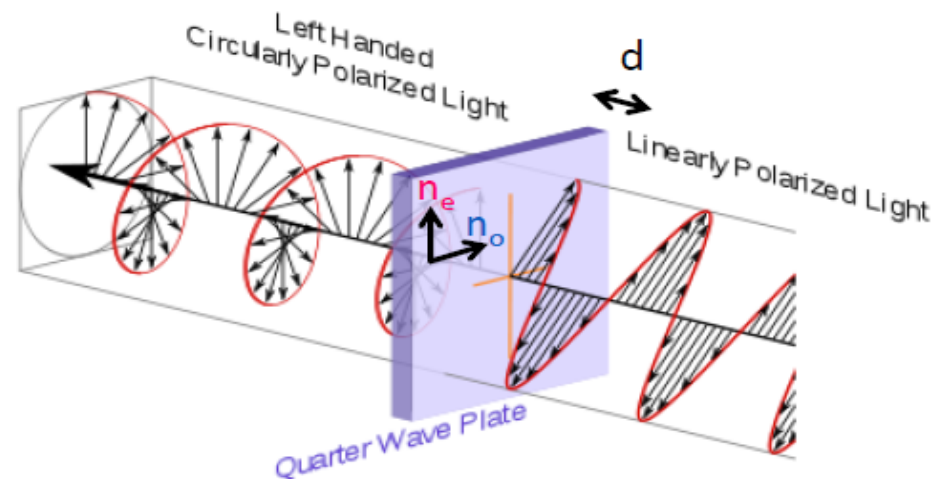
# CONVENTIONAL OPTICAL COMPONENTS

## Conventional optical components rely on propagation effect

Camera lens (cross-section)



Quarter-wave plate



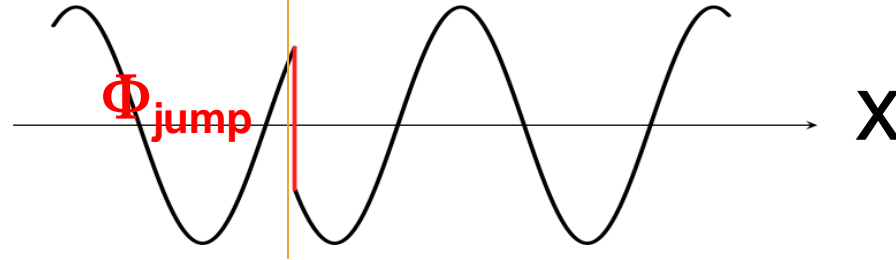
Propagation phase:  $\int_A^B k_o n(r) dr$

Bulk birefringence:  $d |n_e - n_o| = \lambda/4$

What if we introduce in the path a distribution of phase jumps?

# Huyghens metasurfaces: phase “discontinuities”

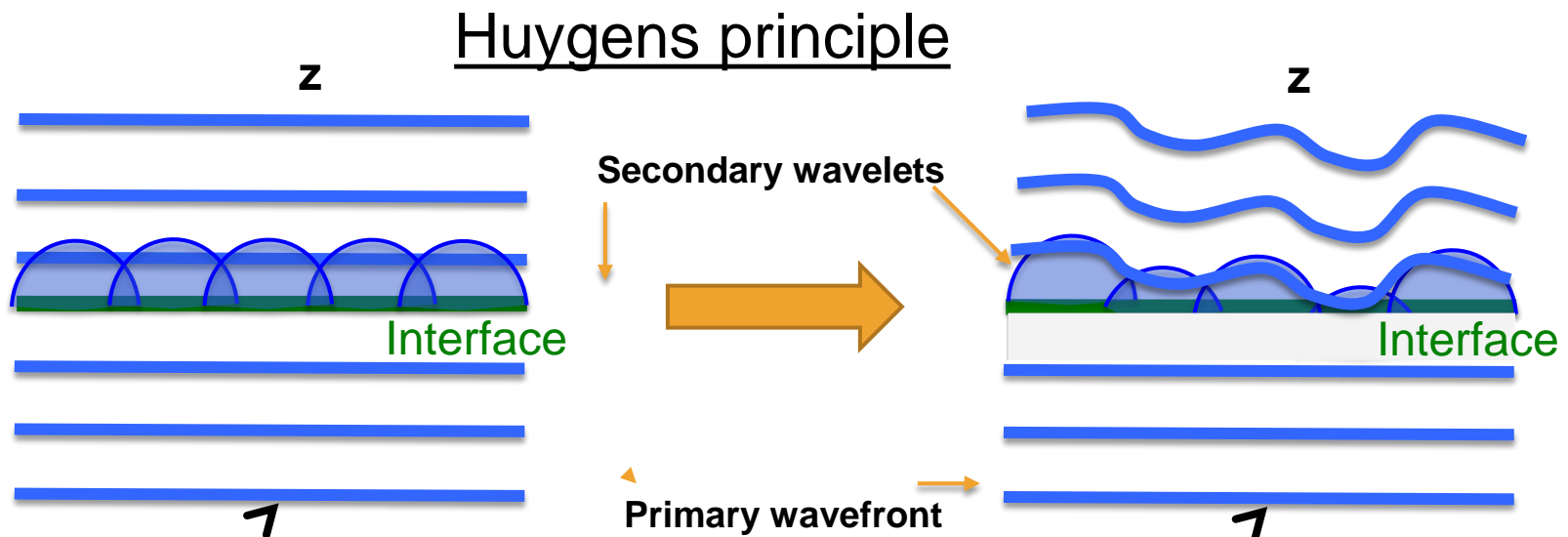
$$A \sin(\omega t - k_y x) \quad A \sin(\omega t - k_x x + \Phi_{\text{jump}})$$



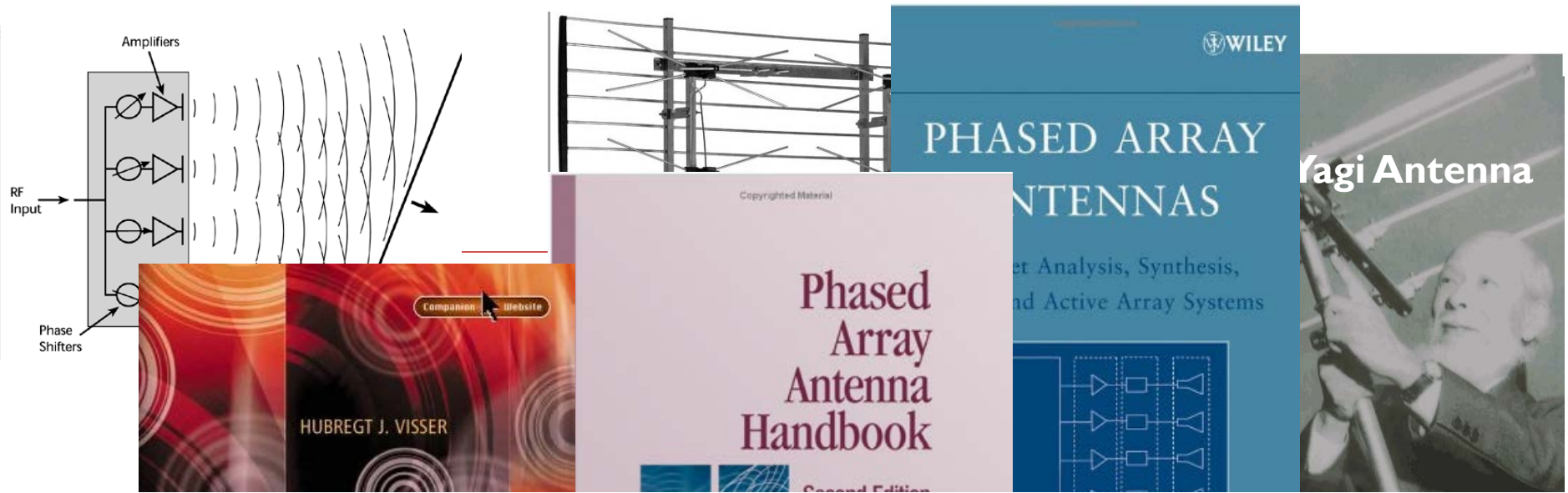
What if could have a spatial distribution of different phase discontinuities along the entire interface?  
→ can make any desired wave front !

How?  
→ Optically thin array of sub-wavelength spaced resonators

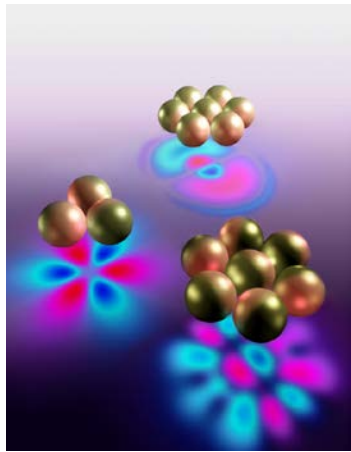
**Any type of resonator: metallic (optical antenna), dielectric, fabry-perot, etc. will do**



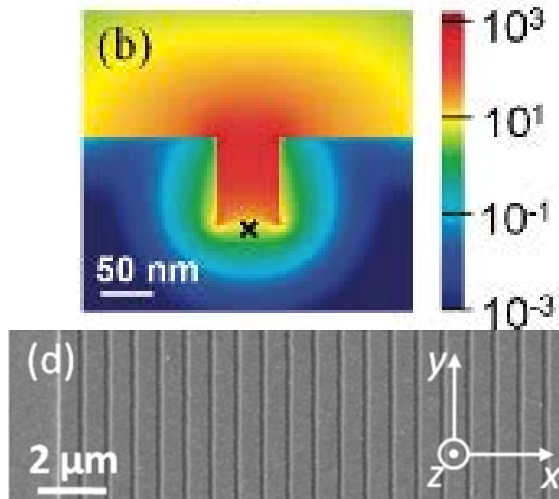
# Phased-array antennas



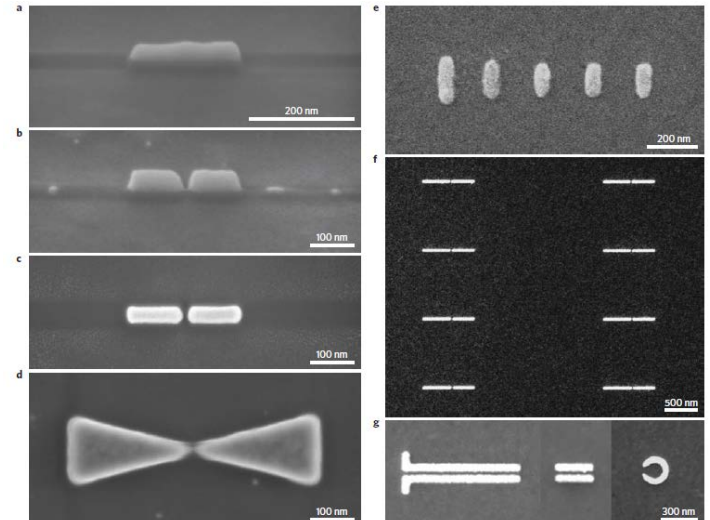
## Phased-array antennas for light



J.A. Fan et al., *Science* 328, 1135 (2010)



P. Genevet et al, *Nano Lett.* 10, 4880–4883 (2010)



L. Novotny et al., *Nature Photon.*, 5, 83



# Gradient Metasurfaces: broadband light bending

Assume a metasurface with a constant gradient of phase delay  
 $d\Phi/dx$

One can easily show that light can be bent in **arbitrary** ways;  
effect is broad band

Generalized Snell's law:

$$\sin(\theta_t)n_t - \sin(\theta_i)n_i = \frac{\lambda_o}{2\pi} \frac{d\Phi}{dx}$$

**Negative refraction**

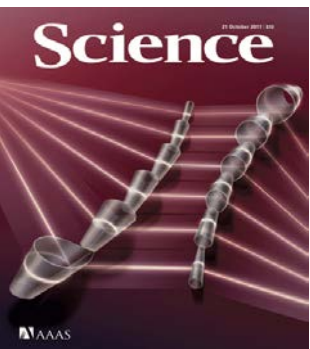
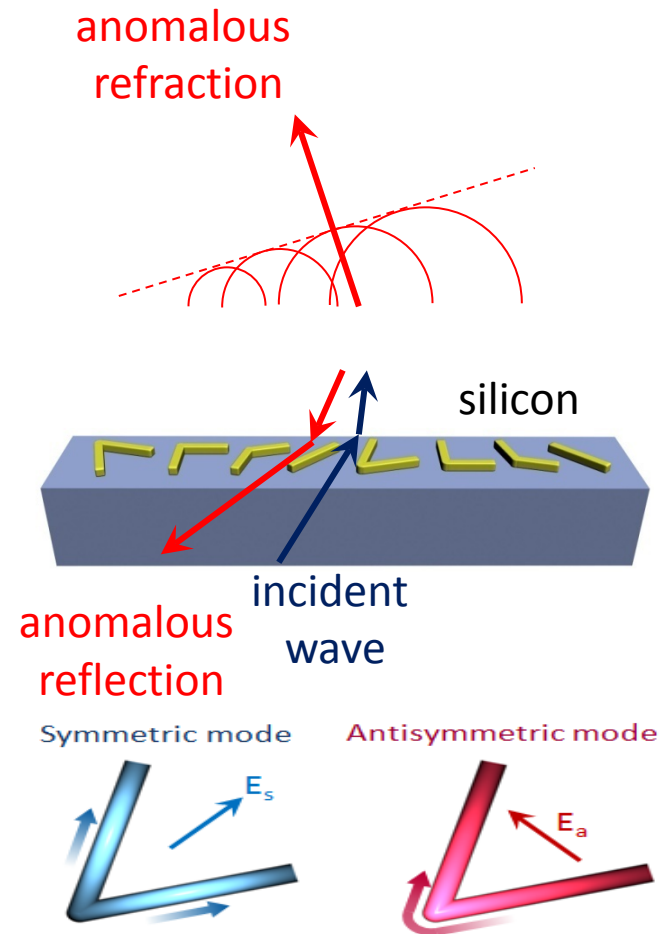
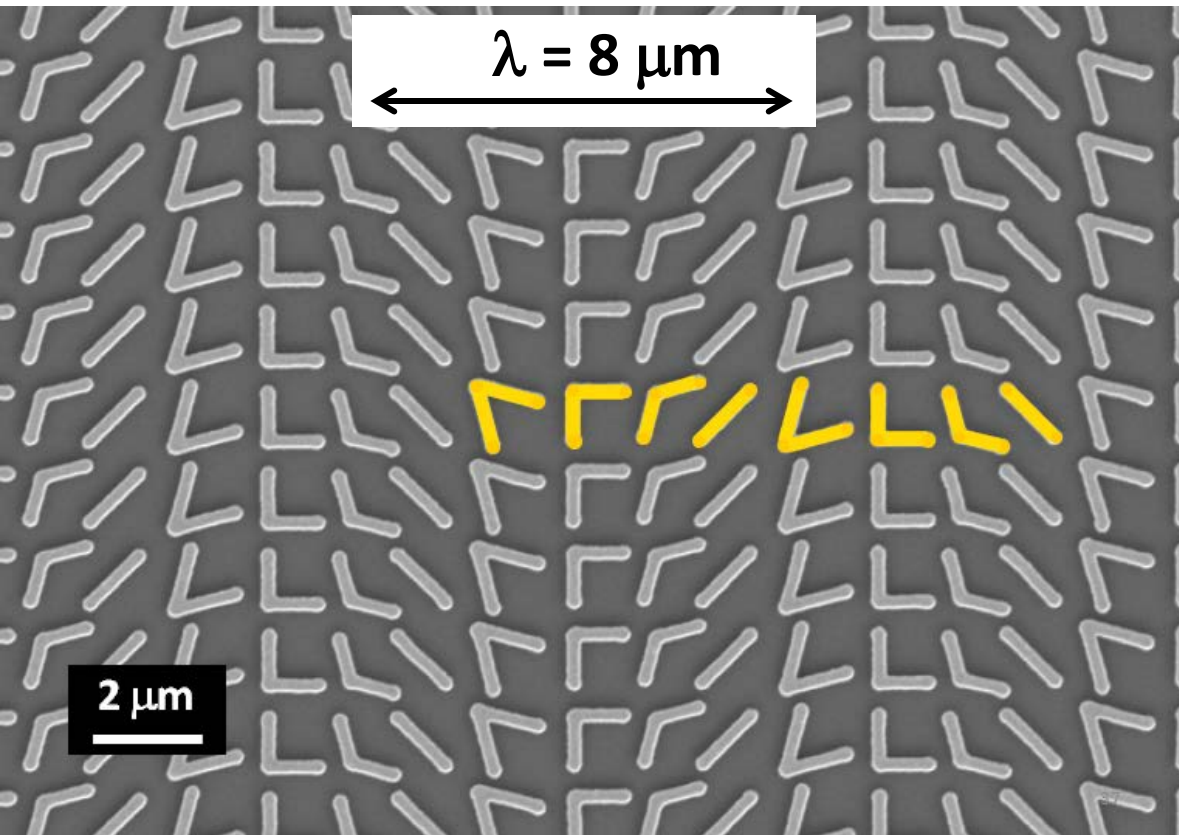
Generalized Law of reflection:

$$\sin(\theta_r) - \sin(\theta_i) = \frac{\lambda_o}{2\pi n_i} \frac{d\Phi}{dx}$$

- **Negative reflection**
- **Critical angle above which no reflection**



# Meta-interface for demonstrating generalized laws



- Optically thin: 50nm
- Subwavelength phase resolution:  $\sim\lambda/5$
- Instant imprinting of a linear phase distribution
- Broadband ( 5-11 microns)

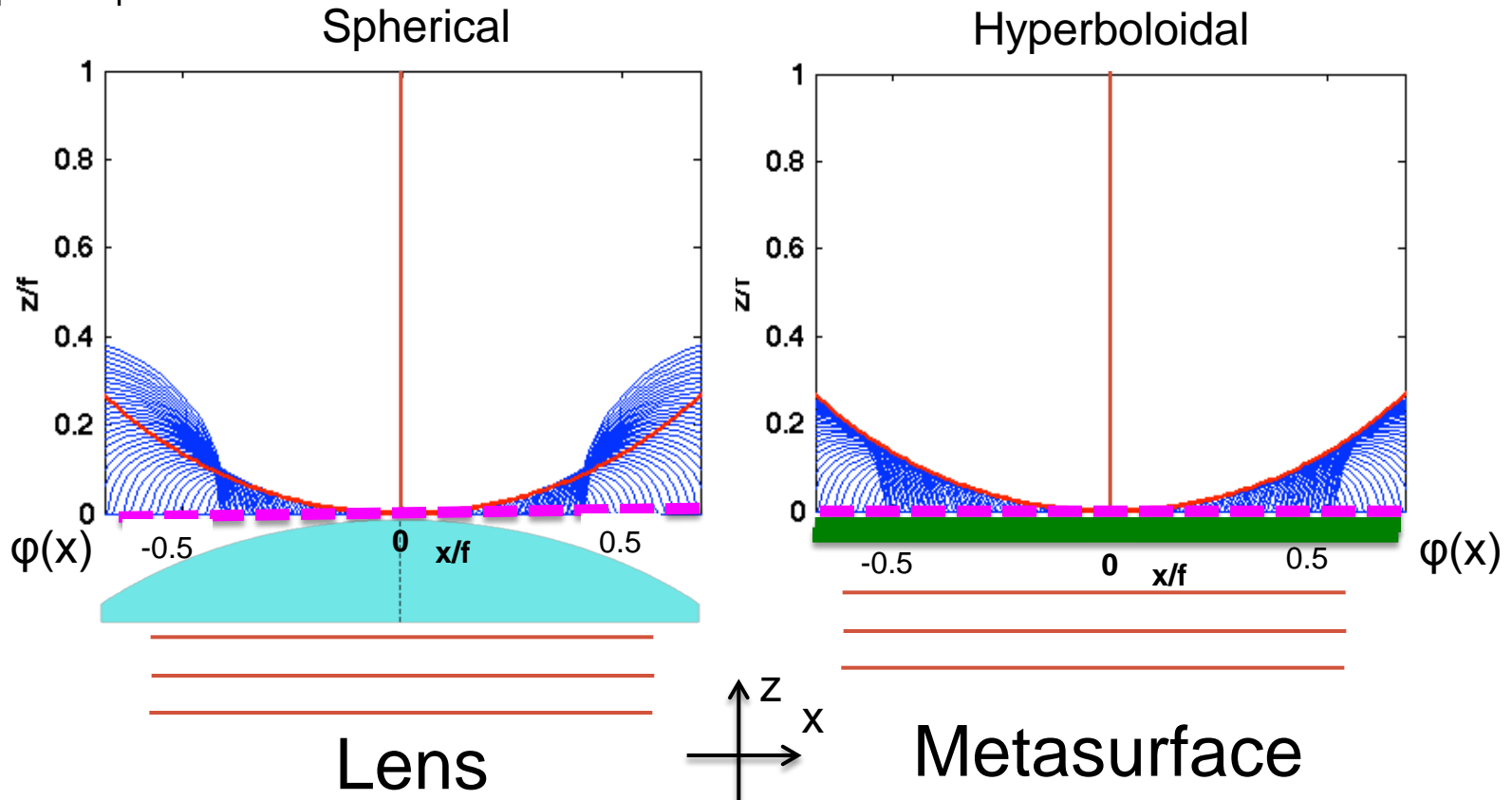
N. Yu *et al.*, *Science* **334**, 333 (2011)

# No Spherical Aberration for flat lens

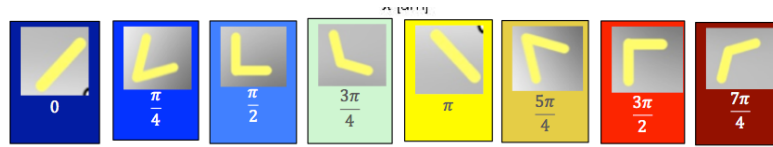
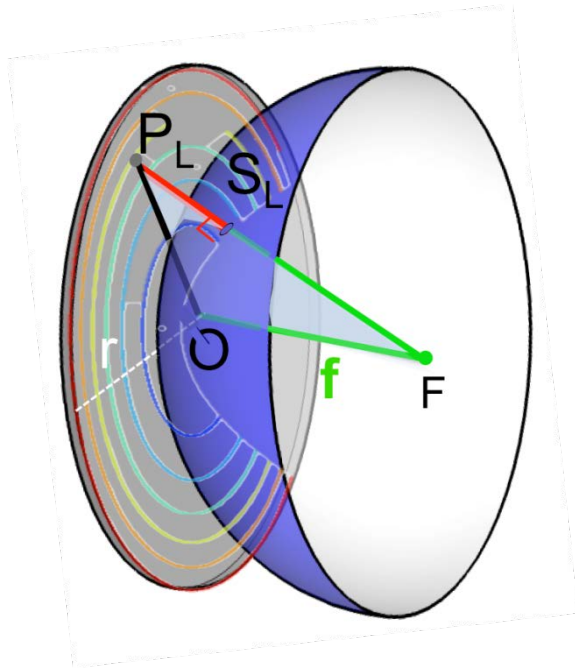
Wavefront = Envelope of Secondary Waves with radii  
 $R(x) = \lambda/2\pi * \varphi(x)$

High N.A. = 0.8

$$\sin\vartheta_i \neq \vartheta_i$$



# METALENS: Flat lens based on Metasurfaces



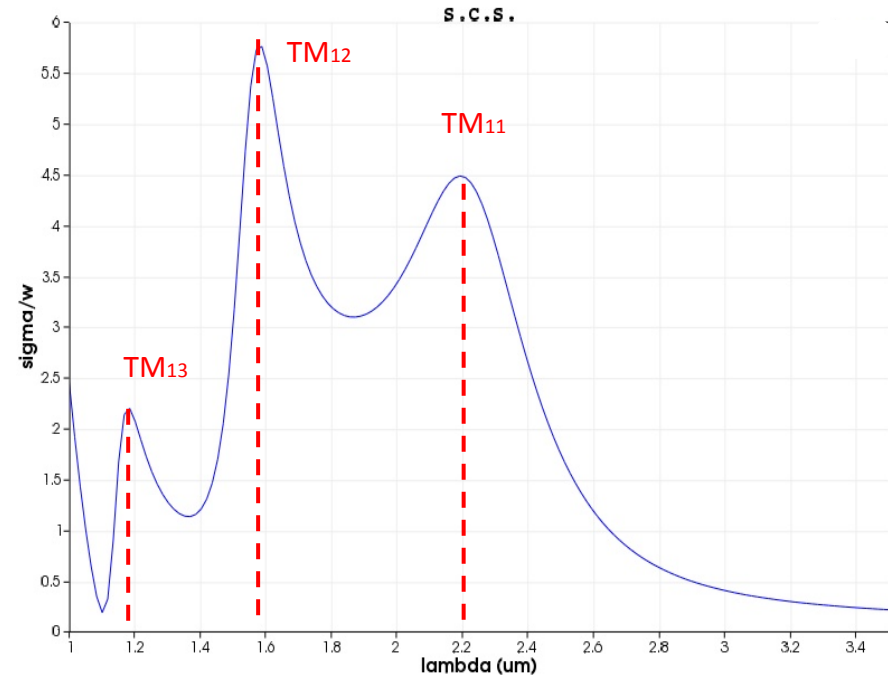
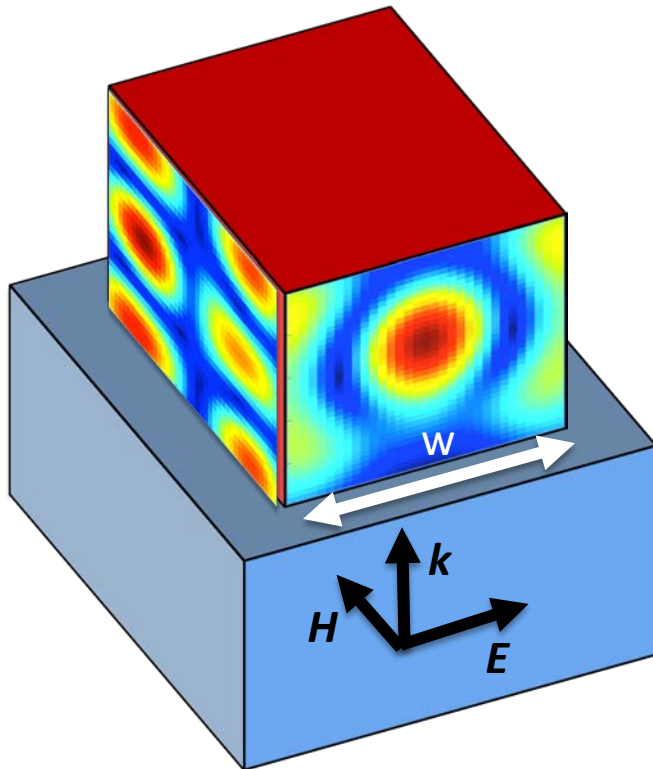
To focus at a certain focal  $f$  the interface must compensate for the distance of every point from a spherical surface centered in the focus and with radius  $f$ .

$$\varphi_L(x, y) = \frac{2\pi}{\lambda} \overline{P_L S_L} = \frac{2\pi}{\lambda} \left( \sqrt{(x^2 + y^2) + f^2} - f \right)$$

**No spherical aberration and large numerical aperture**

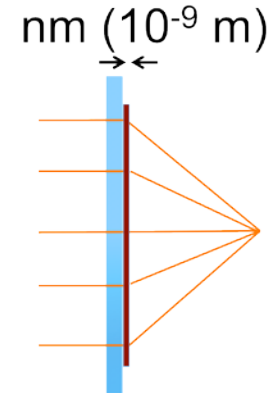
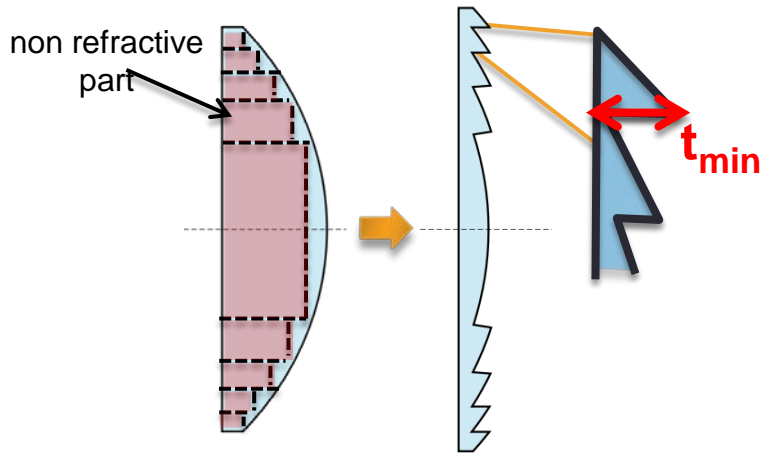
F.Aieta et al. *Nano Letters* **12**, 4932 (2012)

# Dielectric resonators as new building block for tunable metasurfaces



- A simple rectangular dielectric antenna supports multiple modes of resonance that can be used to introduce novel broadband functionalities
- When used at optical frequencies, dielectric materials do not suffer from parasitic optical losses present in metals.
- High scattering efficiency  $\sim 90\%$ . Scattering properties can be tuned by doping and gating standard dielectrics or combining them with phase change materials.

# Fresnel Optics vs Metasurface Based Optics



## Fresnel Optics

thin but finite thickness

finite lateral phase control

polarization insensitive

**diffractive: single wavelength operation**

**multiple steps of lithography:  
N phase level  $\rightarrow$   $\log_2 N$  steps**

## Metasurface

ultra - thin

sub wavelength phase control

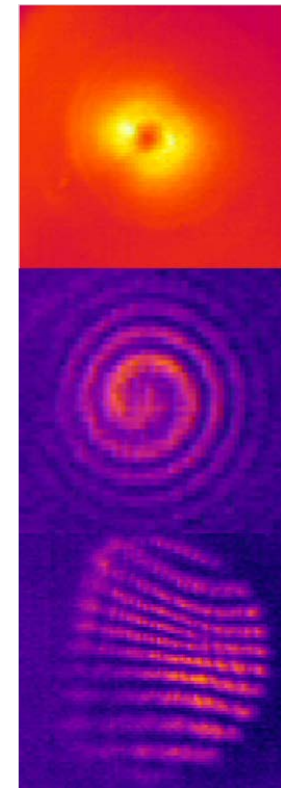
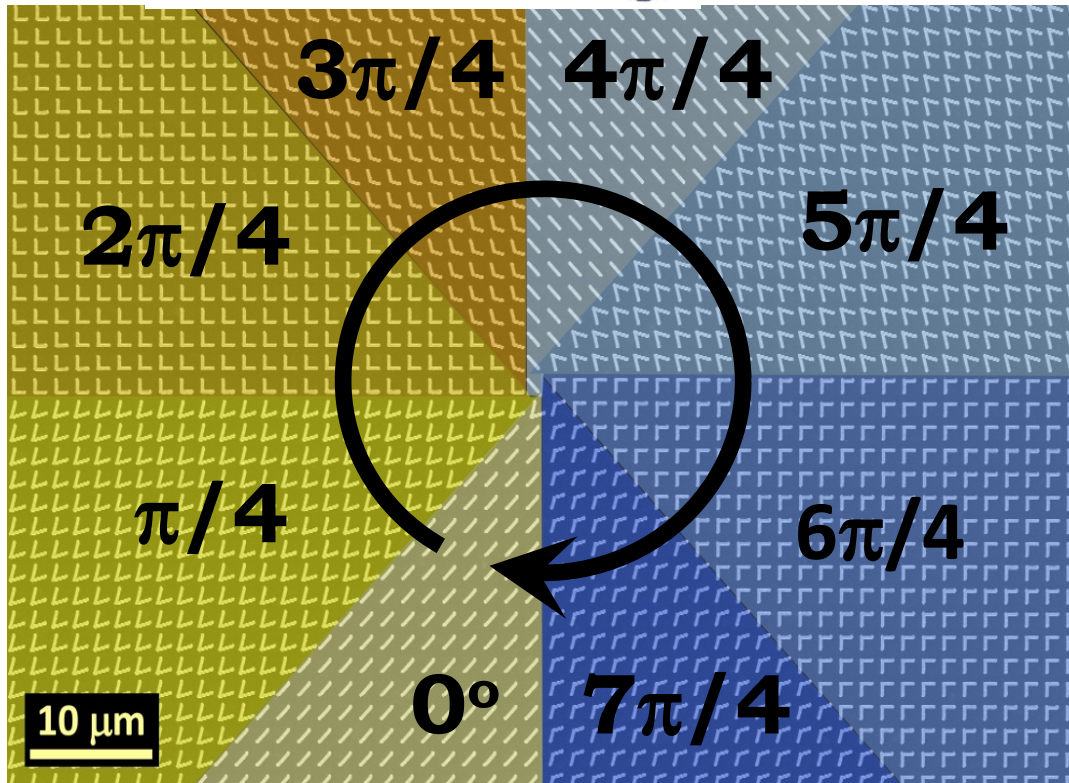
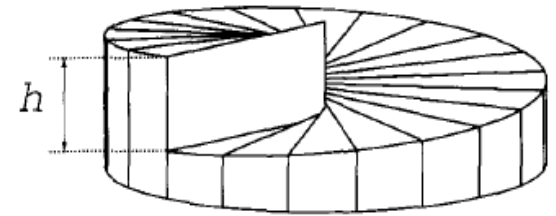
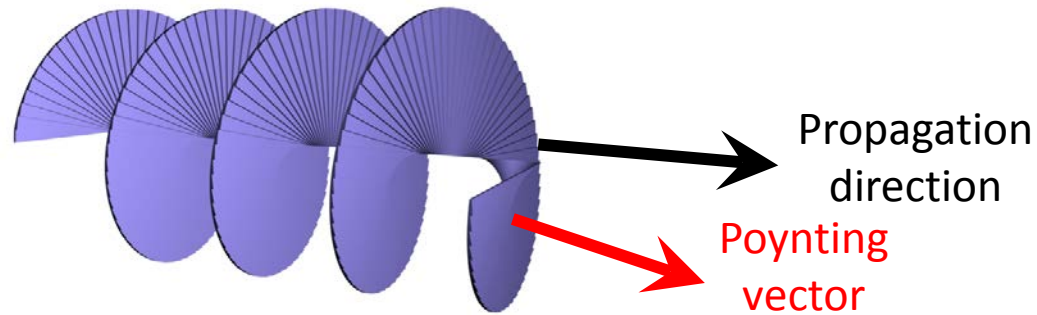
polarization control

**controlled dispersion: achromatic**

**single lithographic step**

**a single digital pattern (one mask level) creates arbitrary analog phase profile !**

# VORTEX PLATE



P. Genevet et al. Appl. Phys. Lett. 100, 13101 (2012)

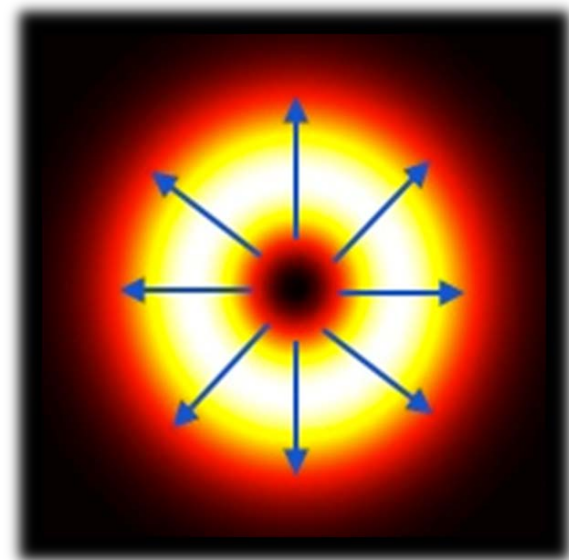
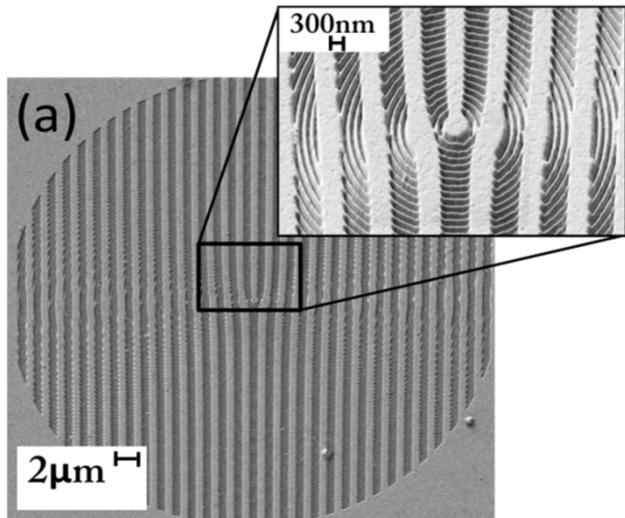
- Radial arrangements create flat lenses ...
- Angular arrangements of antennas create optical vortices

# Nanostructured Holograms for Vector Beam Generation

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**Computer Generated Holograms** is the method of digitally generating holographic interference patterns.

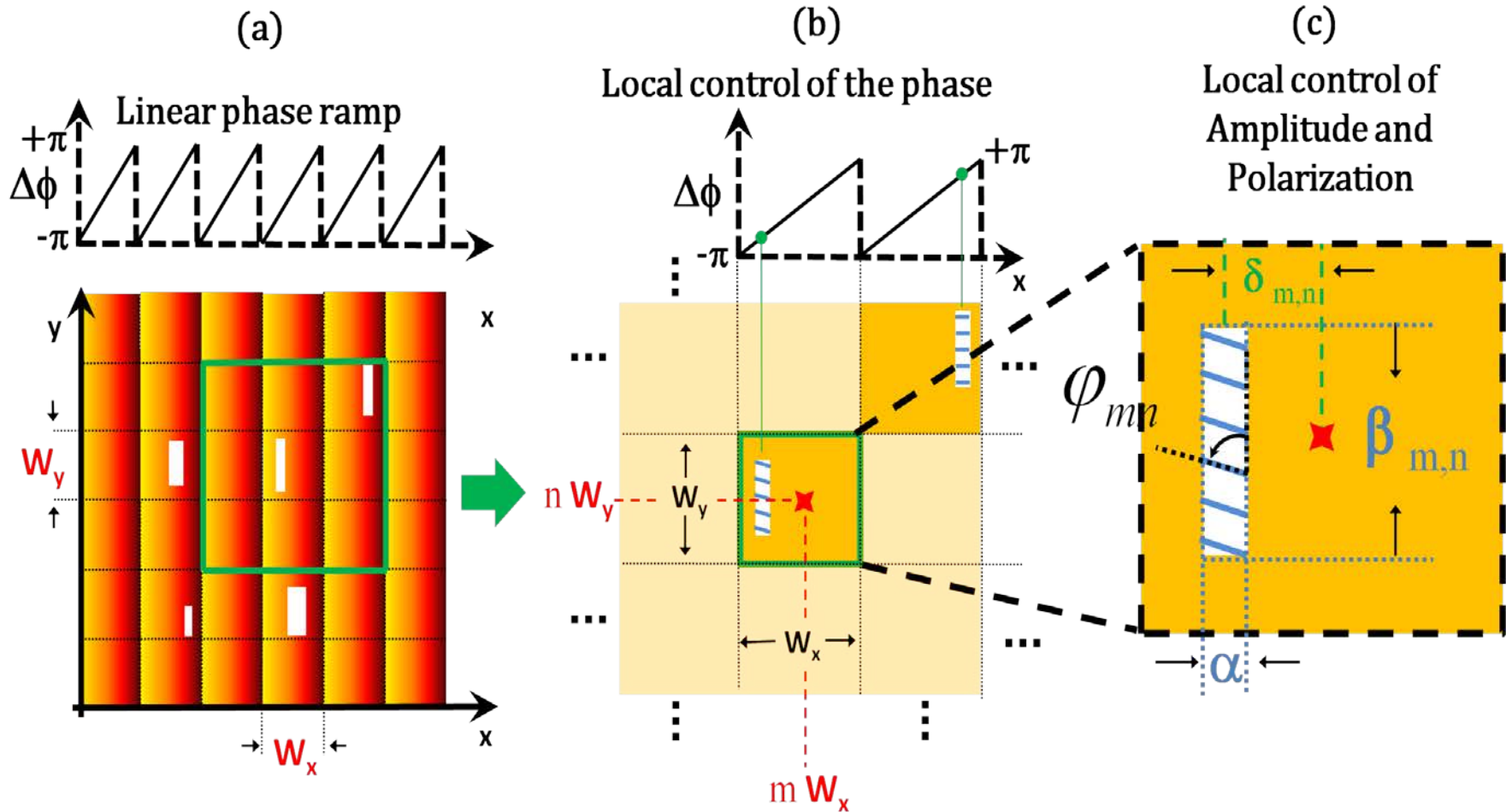
A holographic image can be generated e.g. by digitally computing a holographic interference pattern and printing it onto a mask or film for subsequent illumination by suitable coherent light source.



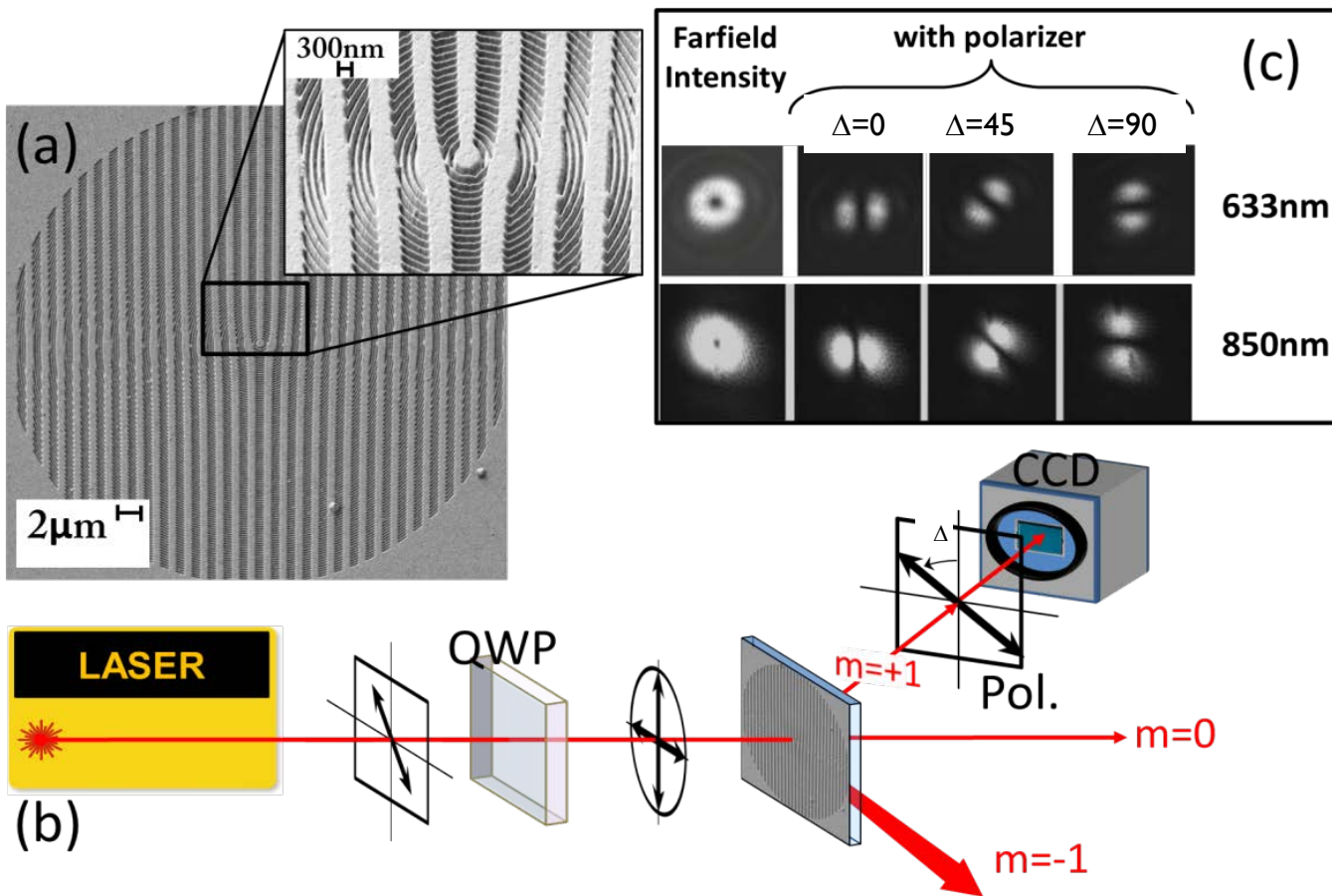


# Nanostructured computer generated holograms for vector beam generation

Vector beam: wavefront with spatially varying polarization



# Nanostructured holograms for broadband manipulation of light



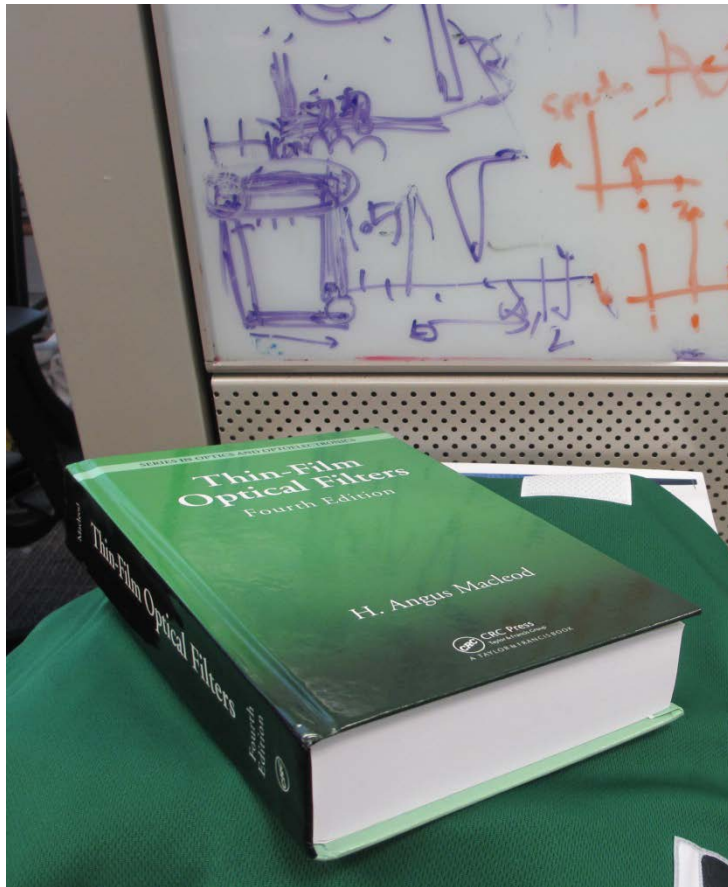
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# Optical interference in films much thinner than wavelength

- ▶ Last half century: a lot of work on optical coatings and filters using thin film interference effects

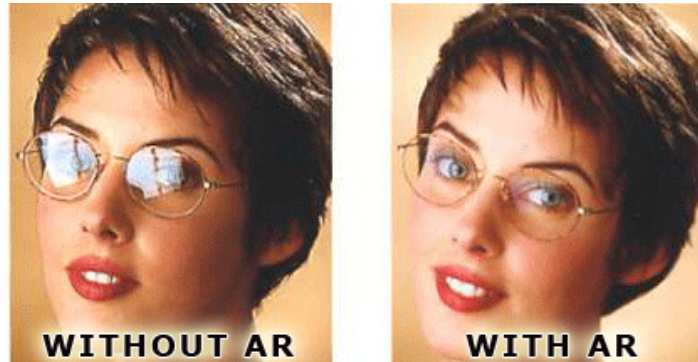


2.8	Potential Transmittance .....
2.9	A Theorem on the Transmittance of a Thin-Film As
2.10	Coherence .....
2.11	Incoherent Reflection at Two or More Surfaces .....
	References .....
3.	Theoretical Techniques .....
3.1	Quarter- and Half-Wave Optical Thicknesses..
3.2	Admittance Loci.....
3.3	Electric Field and Losses in the Admittance Diagram
3.4	The Vector Method .....
3.5	The Herpin Index .....
3.6	Alternative Method of Calculation.....
3.7	Smith's Method of Multilayer Design .....
3.8	The Smith Chart .....

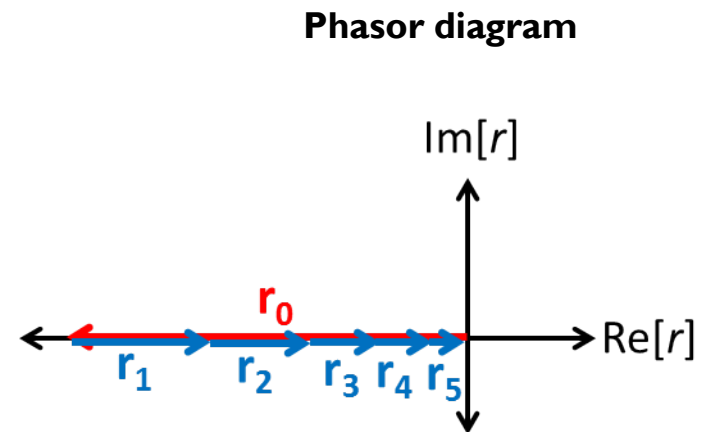
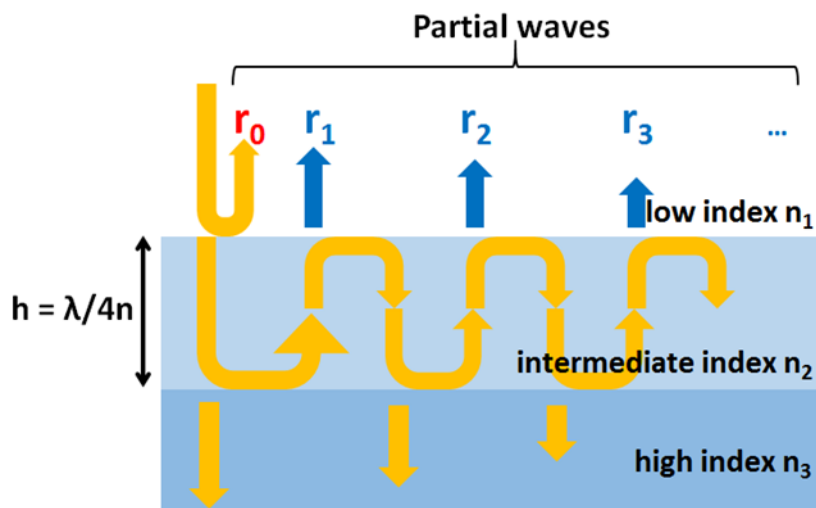
- ▶ Nearly all thin film optical coatings use dielectric layers with **low optical loss** and **thickness on the order of a wavelength**

# Anti-reflection (AR) coating

- ▶ A simple application: anti-reflective coatings

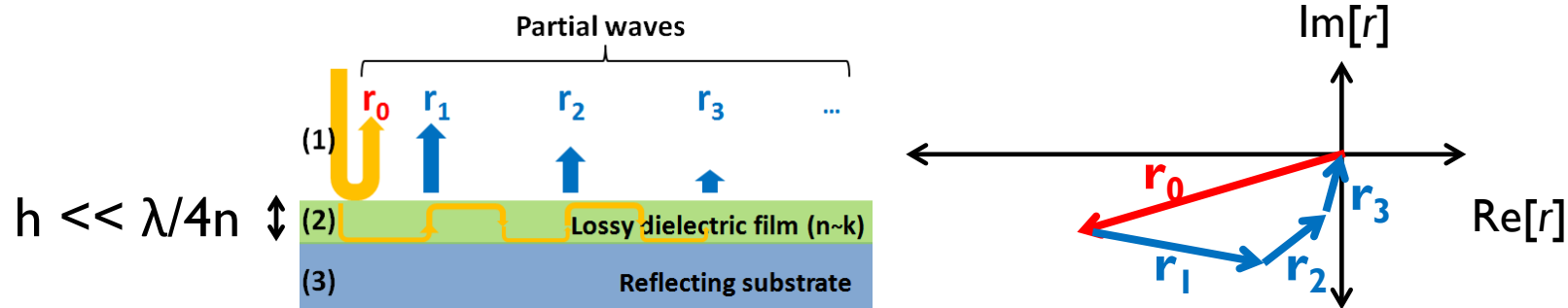


- ▶ Simplest/thinnest conventional AR coating: quarter-wave ( $\sim 50 - 150$  nm in the visible) film (optimized for a particular wavelength)



# Lossy dielectrics and metals

- ▶ Metals with finite conductivity and lossy dielectrics have weird interface reflection phase shifts (i. e. not 0 or  $\pi$ )
  - ▶ Different interference condition compared to the lossless case:  
“**resonance**” can exist for films significantly thinner than  $\lambda/4$

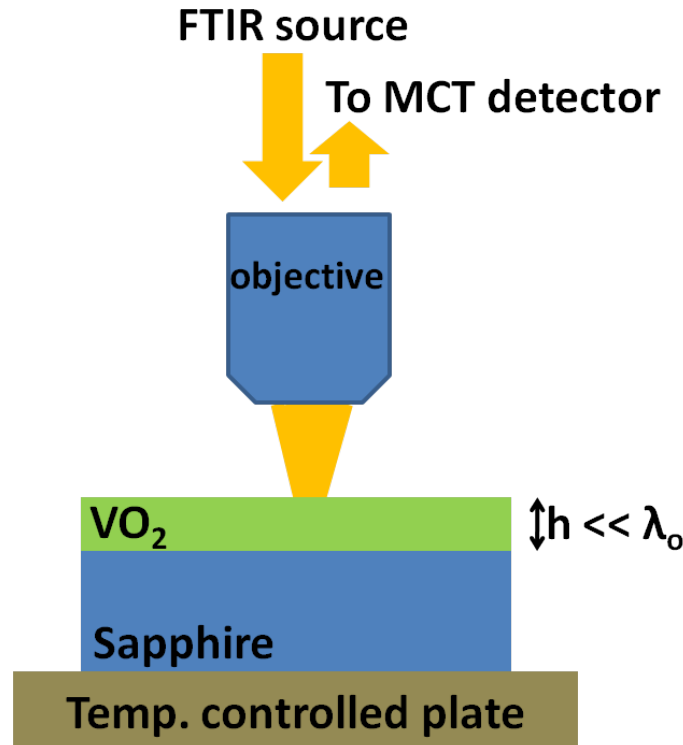


- ▶ Takeaway message: it is possible to **suppress reflection ( perfect absorber)** by using **coherent effects** in a system involving an **ultra-thin, highly-lossy layer**

# Making a perfect absorber

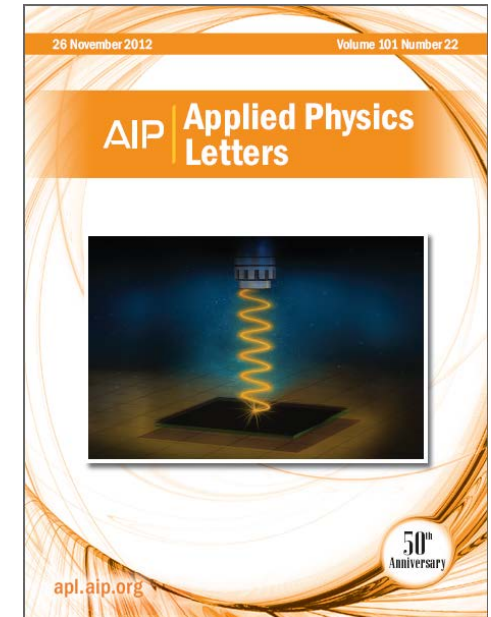
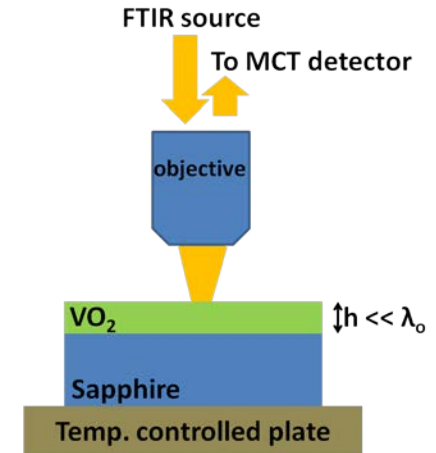
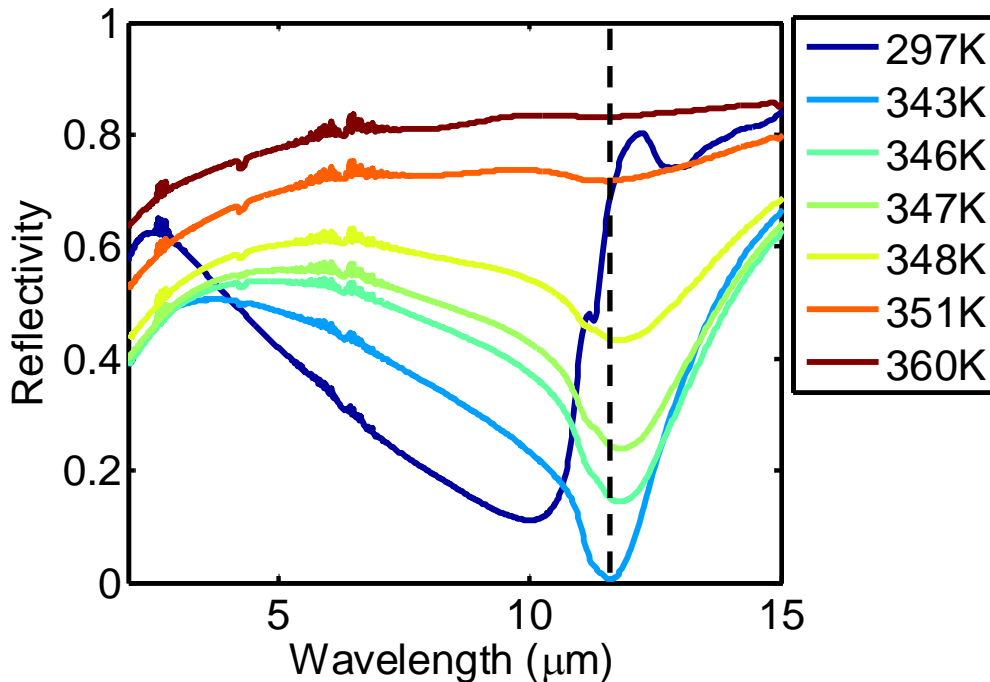
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- ▶ Our experimental system comprises a thin (180 nm vs.  $\lambda \sim 5\text{-}15\ \mu\text{m}$ ) film of vanadium dioxide ( $\text{VO}_2$ ) on sapphire
  - ▶  $\text{VO}_2$  serves as highly-absorbing layer (tunable)
  - ▶ Sapphire is highly-reflecting due to phonon activity in the IR



# Perfect absorber

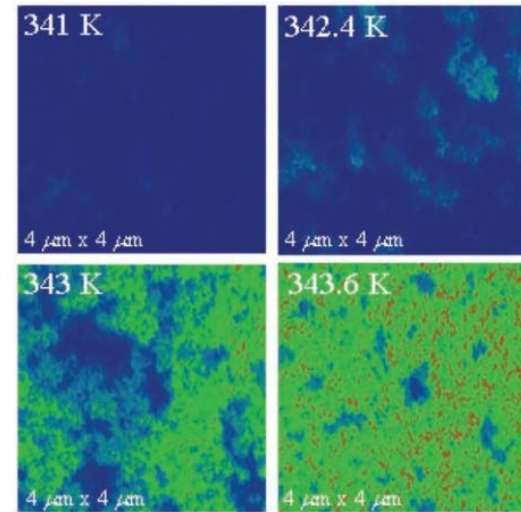
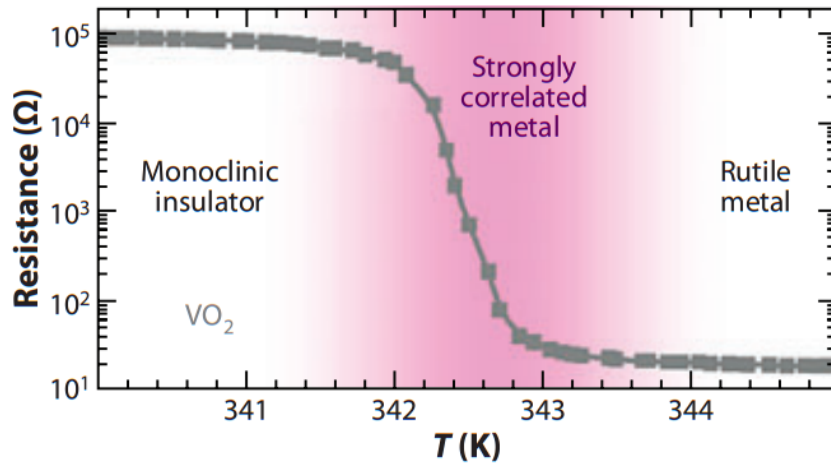
- ▶ Temperature control of  $\text{VO}_2$  allows significant tuning of its refractive index, and hence the sample reflectivity
- ▶ Reflectivity tuning from  $\sim 80\%$  to  $0.25\%$  at  $11.6\mu\text{m}$ 
  - on/off ratio of more than 300
  - entire structure is simply  $180\text{nm}$  of  $\text{VO}_2$  on sapphire





# VO<sub>2</sub> in the transition region

- ▶ What happens in the transition region of VO<sub>2</sub>?

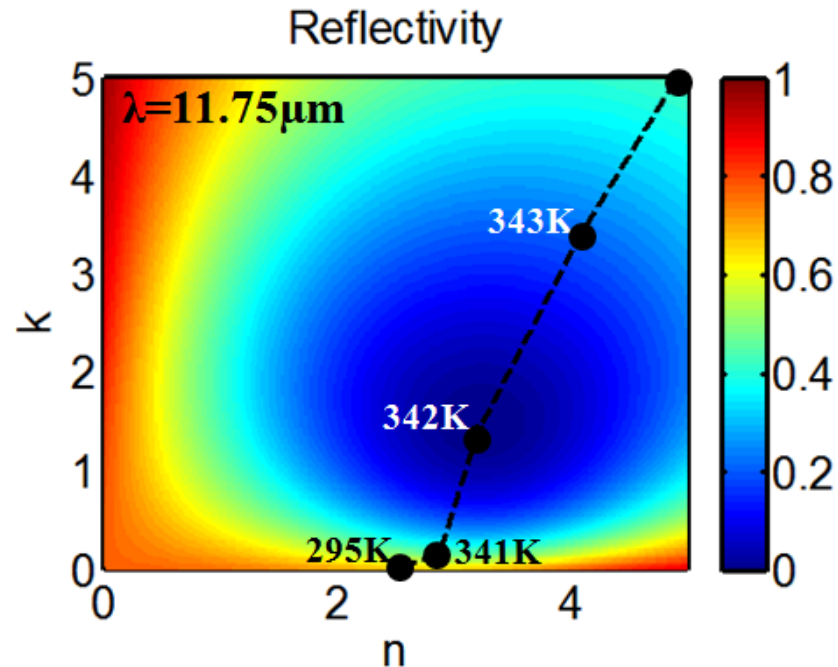


Qazilbash, Basov, et al, Science (2007)

- ▶ Nanoscale islands of metal-phase VO<sub>2</sub> begin to form within a background of dielectric-phase VO<sub>2</sub>, which then grow and connect
  - ▶ The mixture can be viewed as a **disordered, natural metamaterial**
  - ▶ The ratio of co-existing phases can be controlled → **tunable medium**

# Understanding the $R = 0$ condition

- ▶ Fix  $h = 180\text{nm}$ ,  $\lambda = 11.75\mu\text{m}$ , sapphire substrate

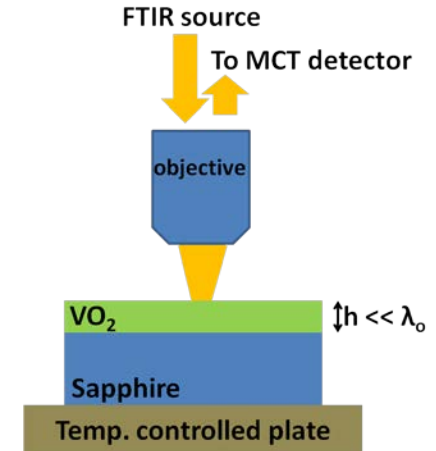


- ▶ VO<sub>2</sub> complex-index trajectory as a function of temperature goes through perfect-absorption condition
- ▶ The minimum is very broad in  $n$ - $k$  space, so the condition is insensitive to small changes in material composition, defects

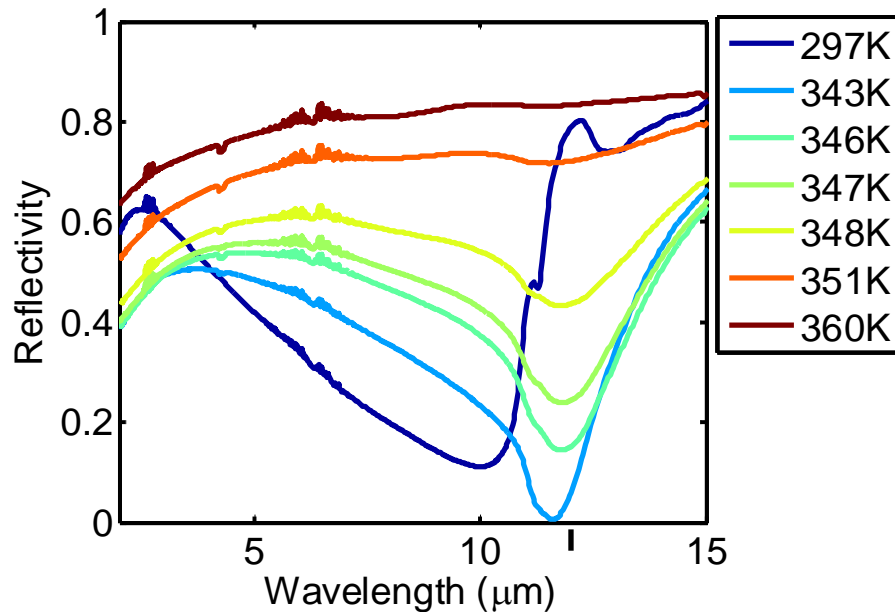
# Perfect absorber

- ▶ Experiment matches analytical calculations
- ▶ Used VO<sub>2</sub> complex index data from Basov group (UCSD)

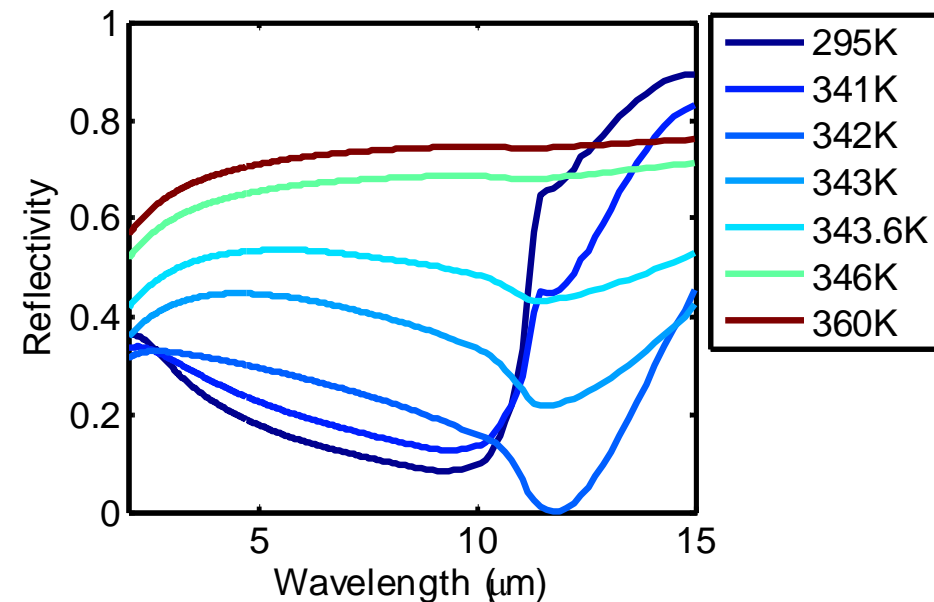
$$r = \sum_{m=0}^{\infty} r_m = \frac{r_{12} + r_{23}e^{2i\beta}}{1 + r_{12}r_{23}e^{2i\beta}}$$



## Experiment

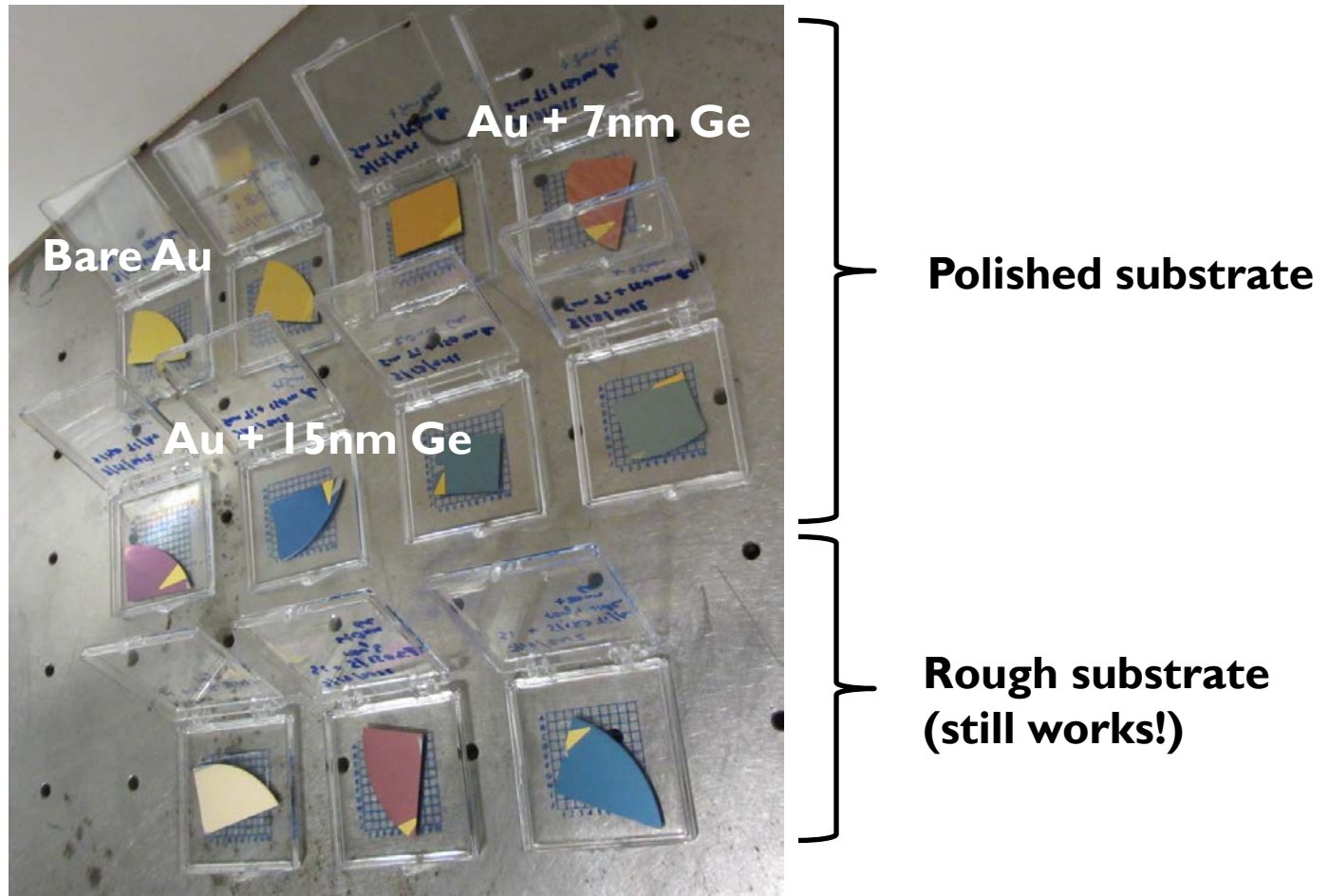


## Calculation



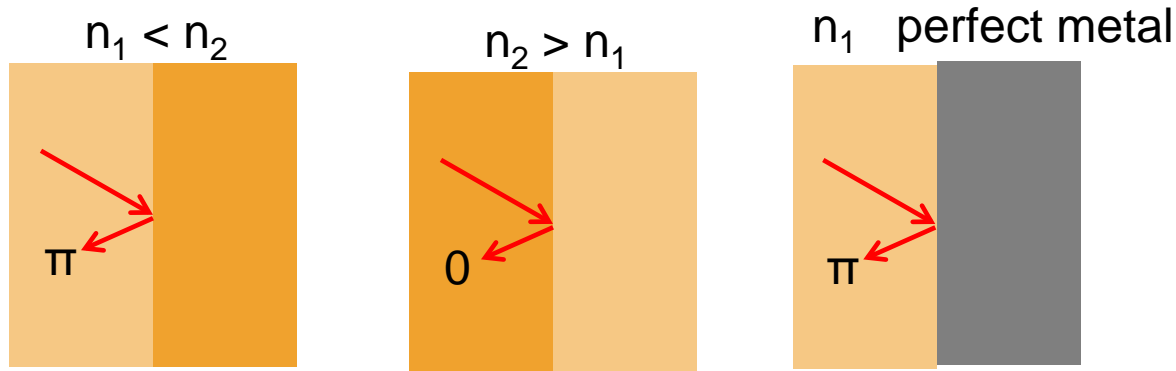
# Coloring gold

- ▶ “Colored” gold films by coating with 5-20 nm germanium films → much thinner than  $\lambda/4$



# Thin film interference in lossy media

- ▶ Thin film interference in highly-absorbing films is unexpected
  1. In the absence of optical loss reflection phase shifts are fixed to either 0 or  $\pi$



- ▶ Lossy materials introduce nontrivial reflection phase shifts
  - ▶  $\rightarrow$  Resonant cavities can be made thinner than  $\lambda/4$
  - ▶  $\rightarrow$  Short propagation lengths allow the use of highly absorbing media

# Questions

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- ▶ Physics and Technology of Disordered Metamaterials?
- ▶ What interesting physics and applications can emerge from embedding quantum effects into metasurfaces? Decorating metasurfaces with single quantum emitters (e.g. NV centers in nanodiamonds)
- ▶ Which large area lithographic technique? Nanoimprint, soft lithography, etc.

# Flat optics

- New class of flat, compact and broadband components: lenses, polarizers., filters, etc.
- High speed tunable phased arrays for real-time wavefront control: role of phase change materials
- Lithography: from Optical to Nanoimprinting and Soft Lithography

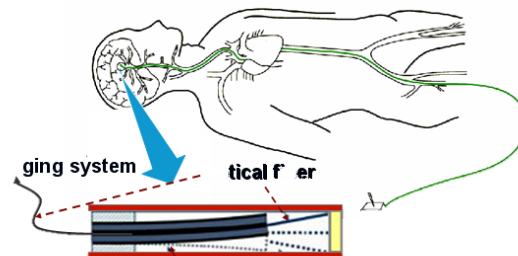
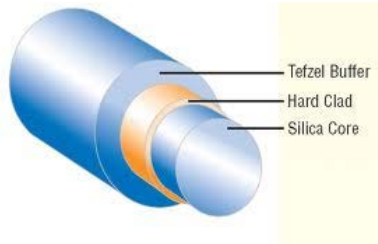


**Smart  
Phones**

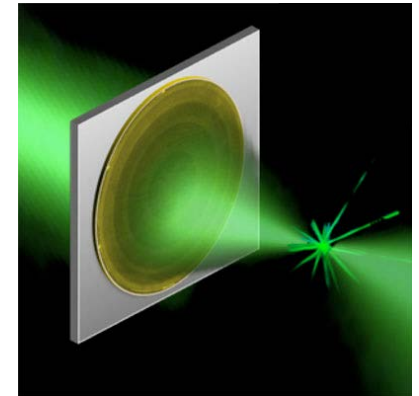
**Stretchable  
Materials**



**Non-Invasive Imaging for  
Biomedical Application**



**High NA  
Objective**



**Major opportunity in  
Midir due to  
poor refractory  
materials**